

Performance evaluation of real-time traffic in aggregate-scheduling networks

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My coauthors

- Joint work with colleagues @ CNG, Pisa
 - Luca Bisti, Luciano Lenzini, Enzo Mingozzi
- Research activity started in 2003
 - 7 conference papers, 4 journal papers



Outline

- Introduction
 - Real-time applications and e2e delay bounds
 - Aggregation in the Internet
 - Problem statement and previous work
- Our method
 - Network Calculus (brief intro)
 - The Least Upper Delay Bound methodology
 - Evaluation: scalability, accuracy
- Conclusions



Real-time traffic

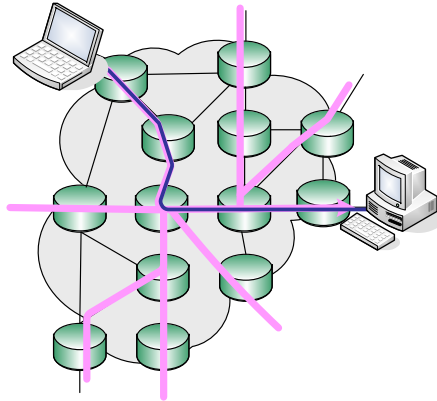
- Expected to represent the bulk of the traffic in the Internet soon
 - Skype users: 10^7 - 10^8
 - Cisco white paper: video traffic volume to surpass P2P in 2010
- Revenue-generating only if reliable
- Reliability boils down to “packets meeting deadlines”
 - End-to-end delay bounds are required



Traffic aggregation

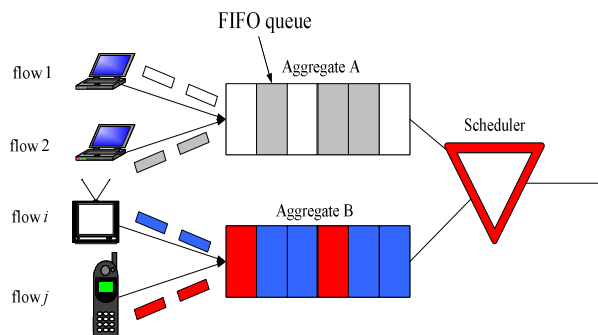
- Aggregation as "the" solution for scalable provisioning of QoS in core networks
- Internet:
 - Differentiated Services
 - MPLS

Per-flow resource management (e.g., packet scheduling) just doesn't scale



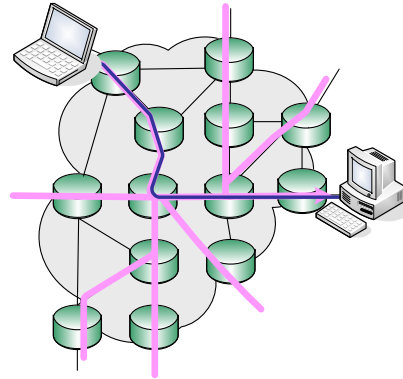
Per-aggregate scheduling

- Packets of an aggregate normally queued FIFO
- Arbitration (scheduling) **among** aggregates
 - Forwarding guarantees **for the aggregate**



Traffic aggregation (cont.)

- Aggregates change along a path
 - Flows join and leave at the nodes
 - Per-node guarantees for **different sets of flows** at each node

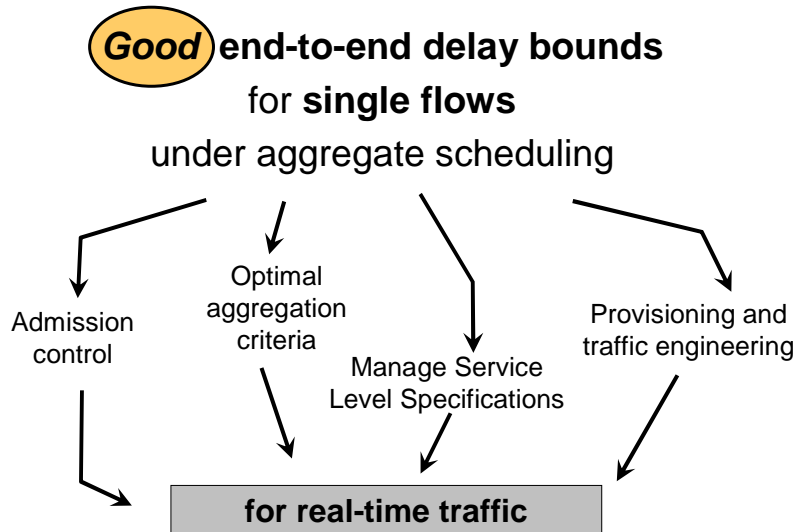


Performance evaluation problem

- Users care about *their flows*, not aggregates
- Users want *e2e delay bounds*, not *per-node forwarding guarantees*

How to compute
per-flow end-to-end delay bounds
from *per-aggregate per-node* guarantees?

Building on the e2e delay bound

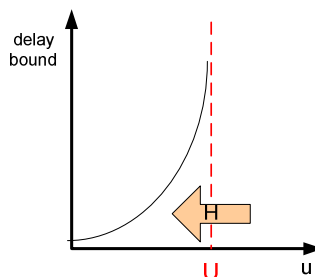


Theoretical background



- Le Boudec, Charny (2001)
 - Generic FIFO network, H hops
 - A delay bound exists
 - For small utilization factors: $u < U = \frac{1}{H-1}$
 - proportional to

$$\frac{1}{1-u/U}$$



- Better bounds require more hypotheses

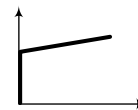
Our approach

- More hypotheses
 - An administrator *does* know the topology of its network
 - Networks are often feed forward
 - Stable up to 100% utilization
 - Compute **better** bounds in practical scenarios
- Tool used: Network Calculus
 - Won't use formulas (promise!)

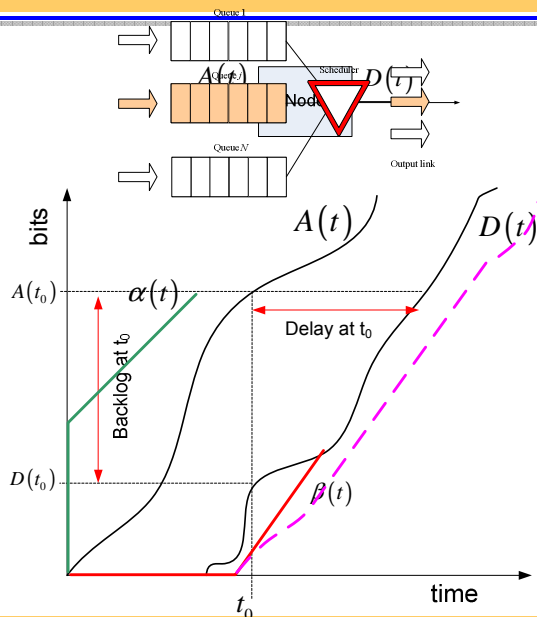


Crash course in Network Calculus (1)

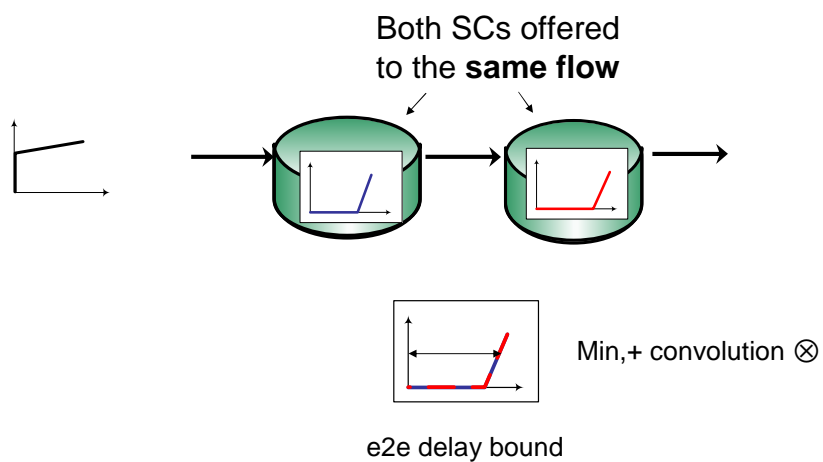
- Model network entities as functions of time or operators on these
 - **Traffic shaper** → **Arrival curve**
 - Upper bound on the arrivals of a flow
 - E.g., a leaky-bucket
 - **Scheduler** → **Service curve**
 - Lower bound on the departures of a flow
 - Per-node forwarding guarantee
 - E.g., a Fair Queuing or Priority scheduler



Crash Course in Network Calculus (2)



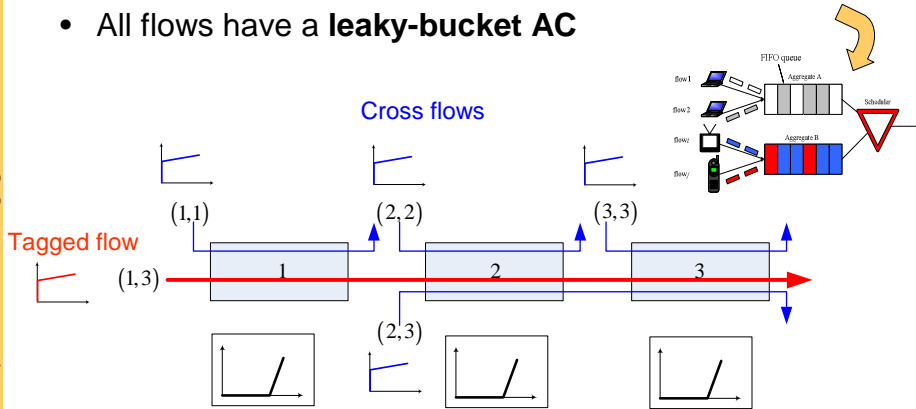
Crash Course in Network Calculus (3)





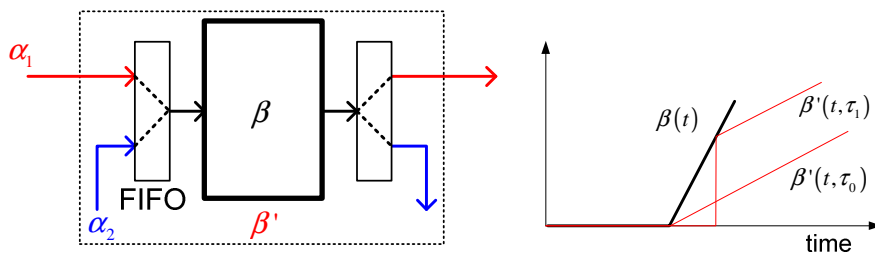
Back to our problem - system model

- **Tandem network** of FIFO rate-latency elements
- All nodes have a **rate-latency SC** for the aggregate
- All flows have a **leaky-bucket AC**

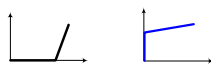


The starting point

- Th. **FIFO Mux - Minimum Service Curves** [Cruz, '98]



$$\beta'(t, \tau) = [\beta(t) - \alpha_2(t - \tau)]^+ \cdot 1_{\{t > \tau\}}, \tau \geq 0$$

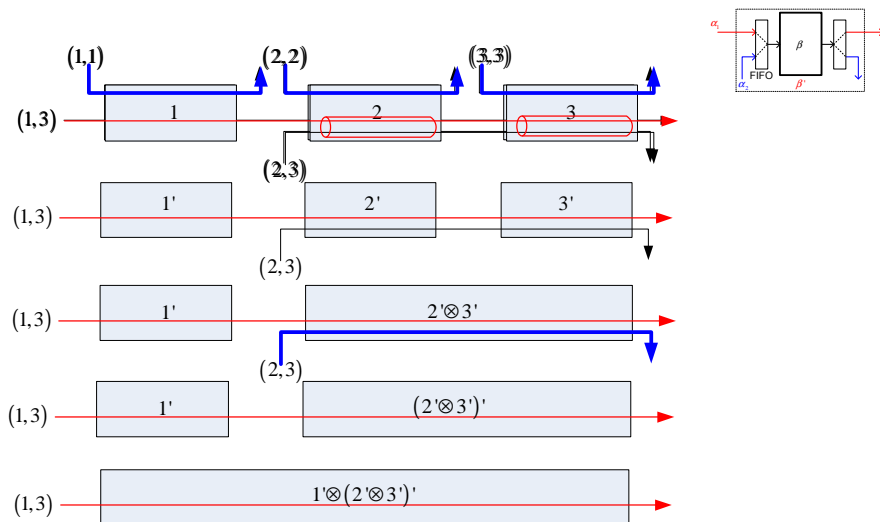


The LUDB methodology

- LUDB: Least Upper Delay Bound
- Step 1:
 - Apply the FIFO Mux theorem iteratively so as to “remove” all cross-flows

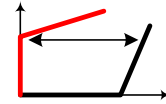


The LUDB methodology (2)



The LUDB methodology (3)

- An **n-dimensional infinity** of e2e SCs for the tagged flow
 - $n = \#$ of cross-flows
- Delay bound = fn. of n parameters
- Step 2
 - Solve an **optimization problem**



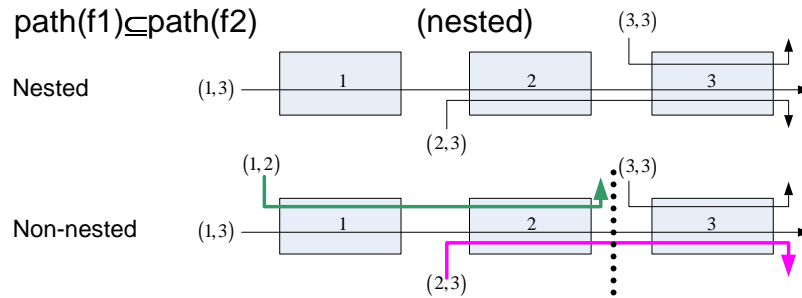
$$LUDB = \min_{\tau_i \geq 0} \{ DB(\tau_1, \dots, \tau_n) \}$$

- The minimum is the **best** delay bound



Nested vs. non-nested tandems

- **Nested iff**
 - $\text{path}(f1) \cap \text{path}(f2) = \emptyset$ (disjoint)
 - $\text{path}(f1) \subseteq \text{path}(f2)$ (nested)



- You can **only** compute an e2e SC for the tagged flow in a **nested tandem**



Two important points

- We show that this method:
 1. Is scalable enough
 - You can use it in paths of 30+ nodes
 2. Yields accurate bounds
 - Close to a flow's **Worst-Case Delay**
 - (Sometimes)
- We start from nested tandem, then move to non-nested ones



Solving the LUDB problem

- Nested tandems

$$LUDB = \min_{\tau_i \geq 0} \{DB(\tau_1, \dots, \tau_n)\}$$

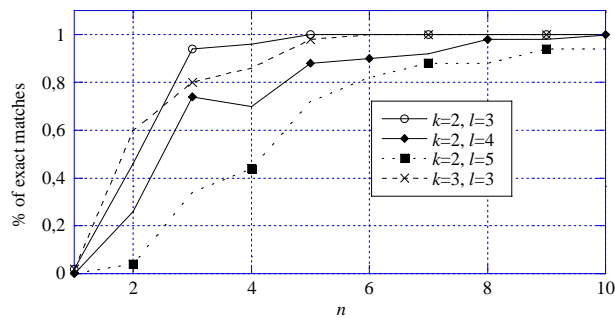
- **Piecewise linear** optimization problem
 - Objective function is piecewise linear
 - Constraints are linear
- We don't know it to be convex
- Equivalent to (a large number of) **simplexes**





Scalability: nested tandems

- 30 nodes: hours, too many simplexes
- Heuristic: try to figure out which (few) simplexes yield the smallest delay bound



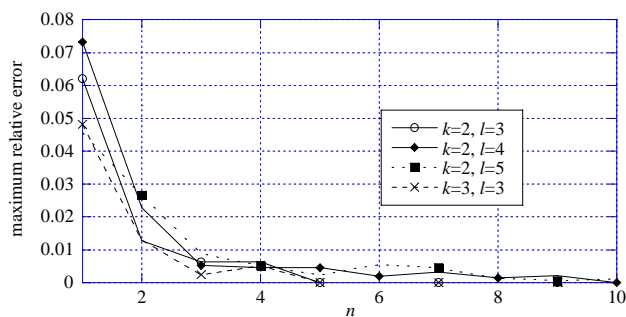
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Scalability: nested tandems

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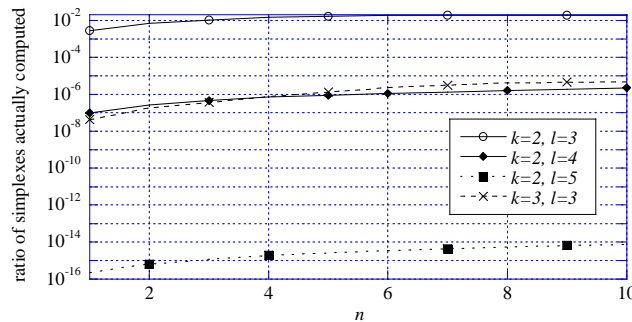
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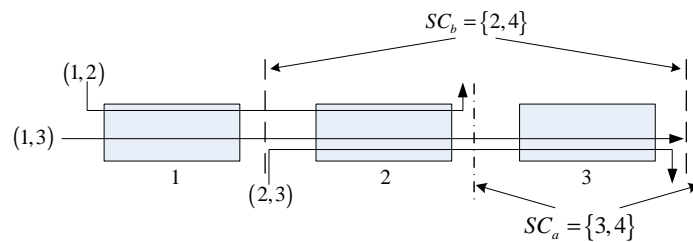
Scalability: nested tandems

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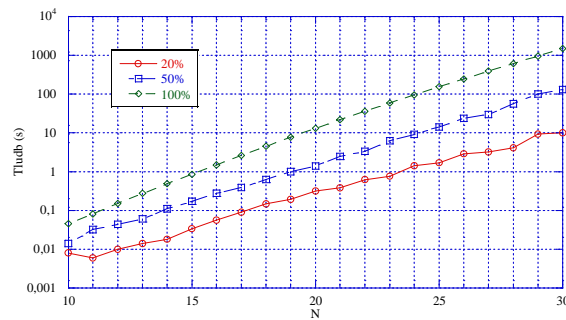
Scalability: non-nested tandems

- Cross-flows are inter-dependent
 - **Cut** the tandem into *nested* sub-tandems
 - Compute the LUDB for the 1st sub-tandem
 - Move on to the 2nd sub-tandem and do the same
 - **Sum** all partial (per sub-tandem) delay bounds
- Problem: many ways to cut a tandem



Scalability: non-nested tandems (2)

- Identify only **good** cuts
- Cache and reuse partial LUDB computations



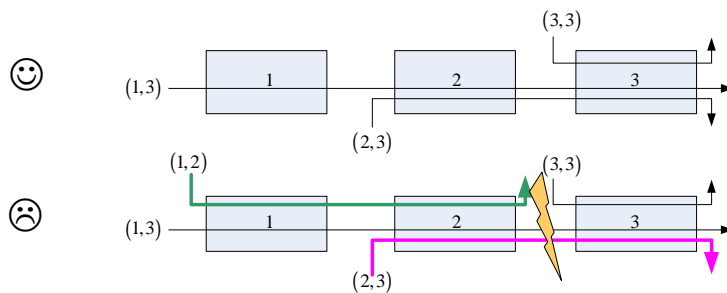
30 nodes, 465 flows, 20 mins

- Computation times for **very nasty** non-nested tandems



Accuracy

- Delay bounds are as useful as they are **tight**, i.e. close to the Worst-Case Delay
 - WCD unknown (to date)
- End-to-end analysis is fundamental



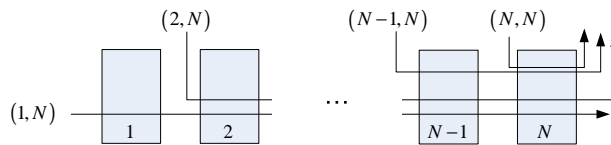


Accuracy (2)

- e2e analysis is however **not sufficient**
 - **Sink trees:** nested tandems, all paths are (j,N)

$$\text{WCD} = \text{LUDB}$$

- Tune flows so that a bit experiences a delay = **LUDB**



- However, in other nested tandems

$$\text{WCD} < \text{LUDB}$$



Assessing the accuracy

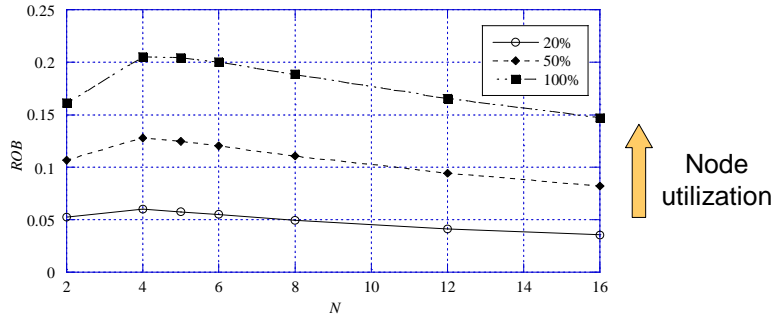
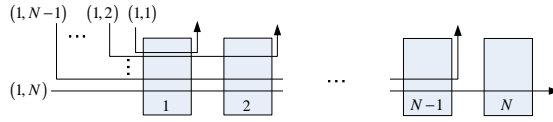
- Compute a (heuristic) **lower** bound
 - Tune flows carefully so as to “maximize” delay
- Compare the lower bound and the LUDB

$$\text{WCD} \in [\text{LowerBound}, \text{LUDB}]$$

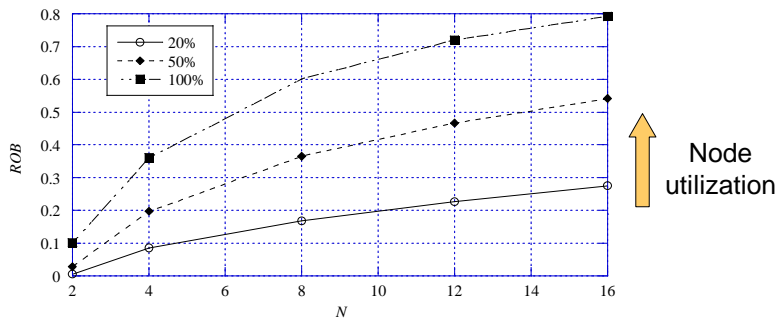
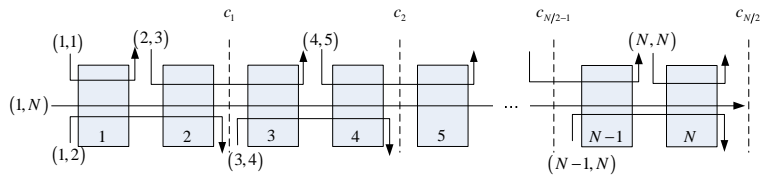
- The smaller the interval, the tighter the bound
- Relative Overrating Bound (ROB):

$$1 - \text{LowerBound}/\text{LUDB}$$

Case Studies - nested tandems

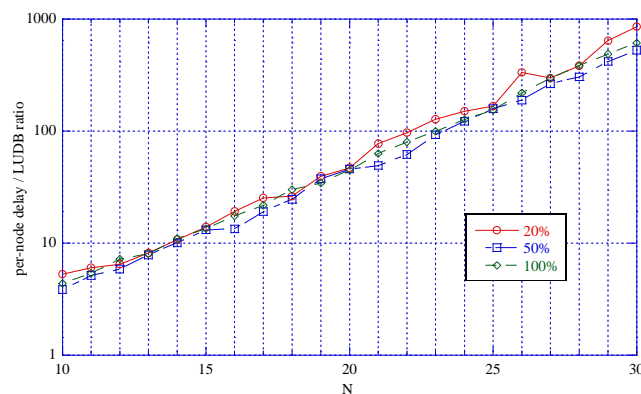


Case studies: non-nested tandems



Still better than the rest

- Compared to (naïve) per-node analysis



500-1000
times smaller

A publicly available tool

- DEBORAH
 - DElay BOund Rating AlgoritHm
 - Includes
 - LUDB computation for nested and non-nested tandems
 - Heuristics for LUDB computation
 - Computation of the *lower* bounds for comparison
 - C++, source code available
- <http://cng1.iet.unipi.it/wiki/index.php/Deborah>

Conclusions

- A method for computing end-to-end delay bounds in FIFO tandem networks
- The method is
 - **Practicable:**
 - analysis of edge-to-edge paths in today ISP's networks requires seconds to minutes
 - **Accurate:**
 - Definitely so in nested tandems
 - Not so much in non-nested tandems



(some) References

1. L. Bisti, L. Lenzi, E. Mingozzi, G. Stea, "Computation and Tightness Assessment of End-to-end Delay Bounds in FIFO Tandems Using Network Calculus", submitted to Elsevier Performance Evaluation, 2008
2. L. Lenzi, E. Mingozzi, G. Stea, "A Methodology for Computing End-to-end Delay Bounds in FIFO-multiplexing Tandems" Elsevier Performance Evaluation, 65 (2008) 922-943
3. L. Lenzi, L. Martorini, E. Mingozzi, G. Stea, "Tight End-to-end Per-flow Delay Bounds in FIFO Multiplexing Sink-tree Networks", Elsevier Performance Evaluation, Vol. 63, Issues 9-10, October 2006, pp. 956-987
4. L. Lenzi, E. Mingozzi, G. Stea, "Delay Bounds for FIFO Aggregates: a Case Study", Elsevier Computer Communications 28/3, February 2005, pp. 287-299
5. L. Bisti, L. Lenzi, E. Mingozzi, G. Stea, "Estimating the Worst-case Delay in FIFO Tandems Using Network Calculus", Proceedings of VALUETOOLS'08, Athens, Greece, October 21-23, 2008
6. L. Lenzi, E. Mingozzi, G. Stea, "End-to-end Delay Bounds in FIFO-multiplexing Tandems", Proc. of VALUETOOLS'07, Nantes (FR), October 23-25, 2007.
7. L. Lenzi, E. Mingozzi, G. Stea, "Delay Bounds for FIFO Aggregates: a Case Study", Proceedings of the 4th COST263 International Workshop on Quality of Future Internet Services (QoFIS '03), Stockholm, Sweden, October 1-3, 2003 LNCS 2811/2003, pp. 31-40



Thank you for listening

- Questions?
- Comments?

